

## CHRONOLOGICAL PUBLICATION LIST

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Papers are listed in chronological order of their initial creation. **Boldface** titles indicate original research results published in refereed research journals, including refereed research-tutorials. Books (except edited books) are listed as “**Boldface in Quotes**”. Other titles include edited books, refereed book chapters, and all non-refereed works. Papers which have been reviewed in *Mathematical Reviews* (MR) or *Zentralblatt für Mathematik und ihre Grenzgebiete* (Zbl.) specify the review locations. All papers are available by mail or email upon request, and most papers are available electronically at the address <http://www.math.gatech.edu/~heil>.

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2. C. E. Heil and D. F. Walnut, **Continuous and discrete wavelet transforms**, SIAM Review, **31** (1989), pp. 628–666. MR1025485. Zbl. 0683.42031.
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- Solutions manual available for instructors, 20 pp.

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- Online course guide, 156 pp.
- Online Chapter 0 (Expanded Notation and Preliminaries), 49 pp.
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