

CHRONOLOGICAL PUBLICATION LIST

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- Solutions manual available for instructors, 20 pp.

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Supplementary material for this text:

- Online course guide, 131 pp.
- Online Chapter 0 (Expanded Notation and Preliminaries), 49 pp.
- Online Alternative Chapter 1 (An Introduction to Norms and Banach Spaces), 62 pp.
- Online Chapter 10 (Abstract Measure Theory), 27 pp.
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- Online Chapter 8 (Integral Operators), 17 pp.
 - Extra online material, 103 pp.
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